

Beware of risk aversion! The role of Probabilistic Sensitivity Analysis in health economic evaluation

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NICE and the cost-effectiveness threshold: Can good intentions compensate for bad practice?

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① Health economic evaluation & PSA

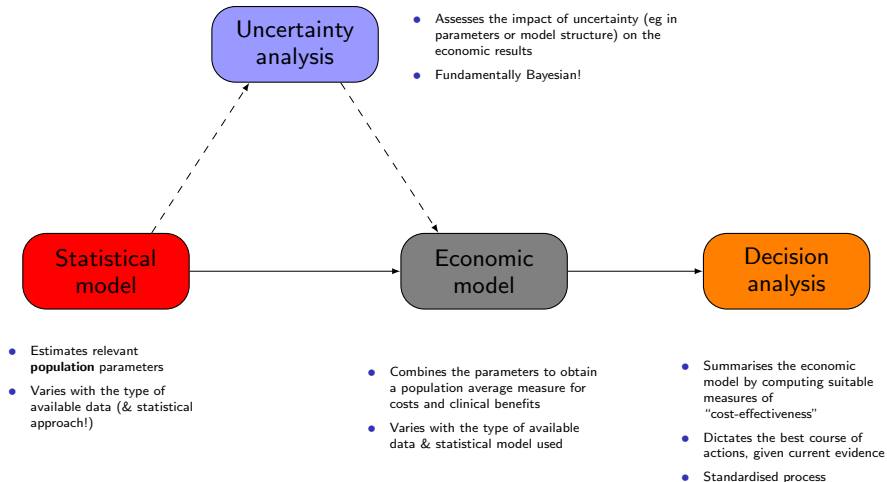
- General structure
- Monetary net benefit
- The nature of PSA

② Risk aversion

- Why?
- How?
- So what?

③ Conclusions(?)

- Potential & limitations
- Open questions



1. Estimation (base-case)

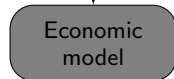
$$\hat{\theta} = f(Y)$$

$$p(y | \theta)$$

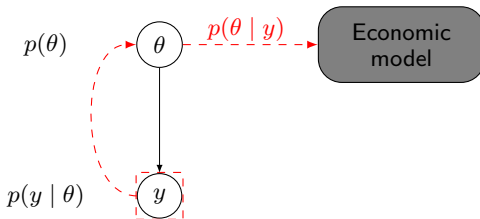


2. PSA

$$p(\theta) \leftrightarrow g(\hat{\theta})$$



Estimation & PSA (one stage)

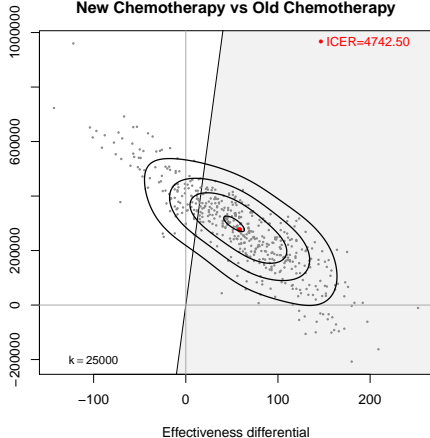


- Typically, we do health economic evaluation based on the **monetary net benefit**

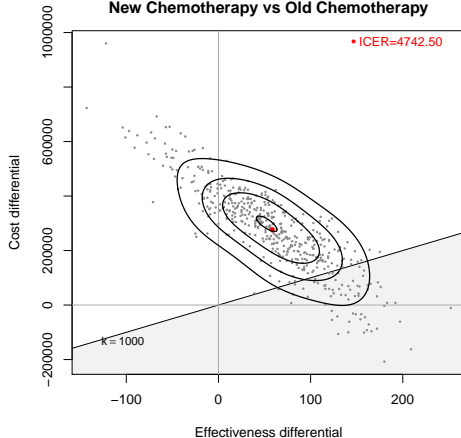
$$u(e, c; t) := ke - c$$

- k is the “willingness to pay”, i.e. the **cost per extra unit of effectiveness gained**
— today’s star!
- The main advantages of using the MNB are that
 - It has a fixed form, once e, c are observed
 - It is a **linear** function in e, c , which simplifies computations
- However, MNB presupposes that the DM is *risk neutral*
 - Of course, that’s not necessarily true
 - However, it **implies** that, given current uncertainty, the DM only requires 50% chance that a treatment is cost effective to deem it so!

**Cost effectiveness plane
New Chemotherapy vs Old Chemotherapy**

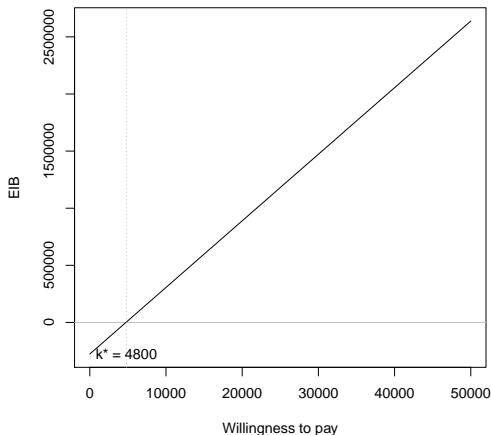


**Cost effectiveness plane
New Chemotherapy vs Old Chemotherapy**



$$\text{ICER} = \frac{E[\Delta_c]}{E[\Delta_e]}$$

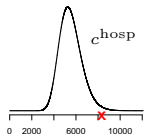
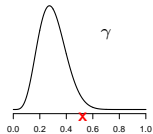
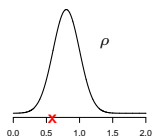
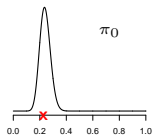
Expected Incremental Benefit



Assuming the MNB as utility:

- $EIB = U^1 - U^0 = E[k\Delta_e - \Delta_c] = kE[\Delta_e] - E[\Delta_c]$
- Thus $EIB > 0 \Rightarrow k > \frac{E[\Delta_c]}{E[\Delta_e]} = ICER = \text{Break even point}$

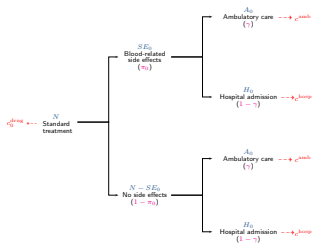
Parameters



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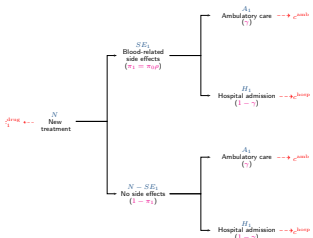
Model structure

Old chemotherapy



⇒

New chemotherapy



Old chemotherapy	
Benefits	Costs
741	670 382.1
699	871 273.3
...	...
726	425 822.2
716.2	790 381.2

New chemotherapy	
Benefits	Costs
732	1 131 978
664	1 325 654
...	...
811	766 411.4
774.5	1 066 849.8

$$\text{ICER} = \frac{276\,468.6}{58.3} = 4\,742.5$$

Iter/n	Parameters simulations				Expected utility		Incremental benefit IB(θ)
	$t = 0$		$t = 1$		$U(\theta^0)$	$U(\theta^1)$	
	Benefits	Costs	Benefits	Costs			
1	741	670 382.1	732	1 131 978.0	19 214 751	19 647 706	432 955.8
2	699	871 273.3	664	1 325 654.0	17 165 526	17 163 407	-2 119.3
3	774	639 071.7	706	1 191 567.2	18 710 928	16 458 433	-2 252 495.5
4	721	1 033 679.2	792	1 302 352.2	16 991 321	18 497 648	1 506 327.0
5	808	427 101.8	784	937 671.1	19 772 898	18 662 329	-1 110 569.3
6	731	1 168 864.4	811	717 939.2	17 106 136	18 983 331	1 877 195.1
...		
1000	726	425 822.2	811	766 411.4	18 043 921	16 470 805	-1 573 116.0
					$U^0=18\,659\,238$	$U^1=19\,515\,004$	EIB= 855 766

Effectively, PSA is based on the comparison between

- The *ideal* decision process — with uncertainty “resolved”:

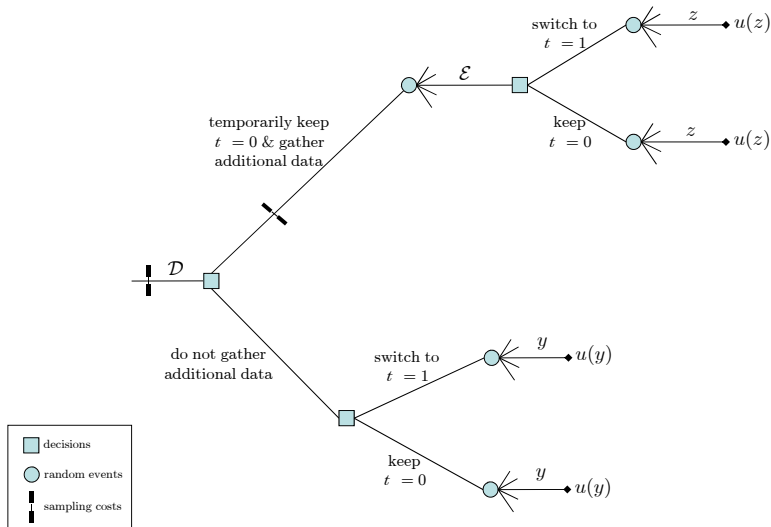
$$U(\theta^t) = k \text{Benefits} - \text{Cost} \quad (\text{under treatment } t)$$

$$= \int u(e, c; t) p(e, c | \theta^t) de dc \quad (\text{expected utility given parameters})$$

- The *actual* decision process — marginalising out all uncertainties:

$$U^t = k E[\text{Benefits}] - E[\text{Costs}] \quad (\text{under treatment } t)$$

$$= \int U(\theta^t) p(\theta^t | e, c) d\theta^t \quad (\text{overall expected utility})$$



- Some times the two steps are actually **conflated**
 - Particularly, given large uncertainty (eg small CEAC), the process is just stopped and marketing authorisation/reimbursement is denied
- Intuitively, this is related to the perceived level of riskiness of a given decision
 - For example, it may be implicitly felt that allowing a treatment with only 65% of cost-effectiveness on the market may be a bad decision
- But:
 - ① The CEAC is only telling one side of the story — how likely is it that the future will turn out very different than the ICER?
 - ② If PSA makes sense in the two-stage decision process (and I think it does!), then the **EVP(P)** is a better tool — also tells about the pay-offs of uncertainty
 - ③ In any case, if riskiness is such a big deal, then the MNB is probably not the best choice for a cost-effectiveness analysis

- Can modify the utility function to formally account for risk-aversion
- This is not a new concept, not even in health economics
 - O'Brien & Schulpher (2000). *Medical Care*, 38:460-468
 - Graff Zivin (2001). *Health Economics*, 10(6):499-508
 - Elbasha (2005). *Health Economics*, 14(5):457-70
 - Baio & Dawid (2011). *Stat Meth Med Res*, doi: 10.1177/0962280211419832
- Can use different forms, **eg**
 - $u_{GZ}(b, r, t) = b - \frac{r}{2} (b - E[B])^2$ $b = ke - c, \quad r < 0$ (Graff Zivin)
 - $u_R(b, r, t) = \frac{1}{r} [1 - \exp(-rb)]$ $b = ke - c, \quad r > 0$ (Raiffa)
- In both cases, b is the MNB, while r is a parameter of **risk-aversion**
 - In the first case: $\downarrow r \Rightarrow$ DM is more risk-averse
 - In the second one: $\uparrow r \Rightarrow$ DM is more risk-averse

- The quantities we need to investigate for PSA are

$$\begin{aligned}U_{GZ}(\theta^t) &= \mathbb{E}[u_{GZ}(b; t, r) \mid \theta^t] = \int \left[b - \frac{r}{2}(b - \mathbb{E}[b])^2 \right] p(b \mid \theta^t) db \\ &= U(\theta^t) - \frac{r}{2} \text{Var}[B \mid \theta^t]\end{aligned}$$

and

$$\begin{aligned}U_R(\theta^t) &= \mathbb{E}[u_R(b; t, r) \mid \theta^t] = \int \frac{1}{r} [1 - \exp(-rb)] p(b \mid \theta^t) db \\ &= \frac{1}{r} [1 - M_{B|\theta^t}(-r)]\end{aligned}$$

- **Complex mathematical form — no longer linear!**
- However, can get them as a by-product of MCMC estimation (in a fully Bayesian setting)

$$U_{GZ}(\theta^t) = U(\theta^t) - \frac{r}{2} \text{Var}[B | \theta^t]$$

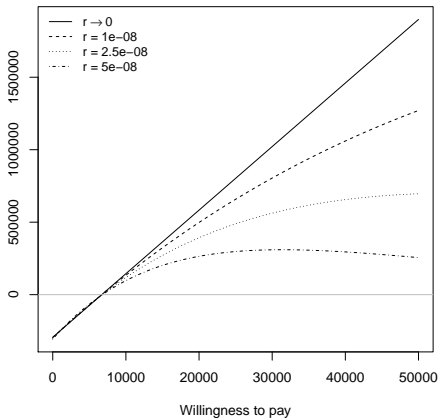
- Obviously, when $r = 0$, then $U_{GZ}(\theta^t) = U(\theta^t)$
- The additional term (involving r) can be considered as some sort of *penalty* — the larger the variability in the MNB, the lower the overall utility
- **Drawback:** need to obtain both the population average and variance of costs and benefits from the statistical model, in order to use GZ

$$U_R(\theta^t) = \frac{1}{r} [1 - M_{B|\theta^t}(-r)]$$

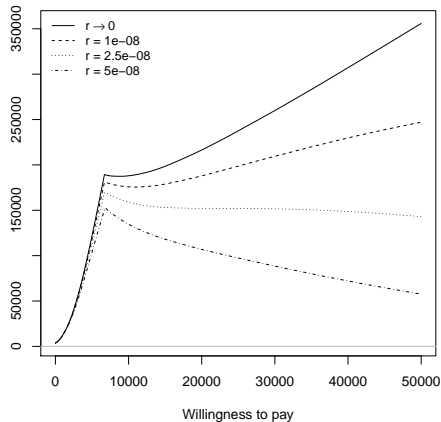
- Not intuitive — but can prove that for $r \rightarrow 0$ then retrieves the MNB
- **Advantage:** only need to obtain the population average costs and benefits from the statistical model (that's what we normally have!)
- In addition, the EVPI is appropriately sensitive to the choice of r , but the CEAC is not, using this utility

- **Main complication:** In any case, it is difficult to determine the scale of r

EIB as a function of the risk aversion parameter



EVPI as a function of the risk aversion parameter



- The choice of the utility function is instrumental to the economic evaluation
 - Assuming the MNB implies risk neutrality — but we do not always mean that!
- If riskiness is a big deal (eg MenB vaccine?), then it would be appropriate to include a form of risk aversion in the model
 - This would be in contrast to modifying the cost-effectiveness thresholds *post-hoc*
 - Utility functions including risk aversion will typically modify the break-even point and thus the decision under current evidence
 - Most likely, the results of PSA are affected too
- It is objectively difficult to elicit the level of risk aversion
 - In general we understand the limiting value and the sign of r
 - But the actual scale (determining how risk averse the decision-maker is) is difficult to determine
 - So what do we do?

Thank you!